

6.4 Inverses - an inverse relation interchanges the input and the output values of the original function.

Original relation

x	0	1	2	3	4
y	6	4	2	0	-2

Inverse relation

x	6	4	2	0	-2
y	0	1	2	3	4

The graph of an inverse relation is a reflection of the graph of the original relation. The line of reflection is $y = x$. To find the inverse of a relation given by an equation in x and y , switch the roles of x and y and solve for y .

The inverse is a reflection across the line $y=x$.

Jan 28-8:08 PM

How to find an inverse-steps in book

1.) $y = 3x - 5$

Steps

① Switch x and y

$$x = 3y - 5$$

$$+5 \quad +5$$

$$\frac{x+5}{3} = \frac{3y}{3}$$

② Solve for y

$$\frac{x+5}{3} = y = f^{-1}(x)$$

Symbol for inverse $f^{-1}(x)$

P
E
M
D
A
S
Work your way up

Jan 28-8:11 PM

Find the inverse of the following function:

① $f(x) = 2x^2 + 1$

$$y = 2x^2 + 1$$

$$x = 2y^2 + 1$$

$$x - 1 = 2y^2$$

$$\frac{x-1}{2} = y^2$$

$$y = \sqrt{\frac{x-1}{2}}$$

$f^{-1}(x) = \sqrt{\frac{x-1}{2}}$

option 2

$$\left(\frac{x-1}{2}\right)^{\frac{1}{2}} = y$$

$$y = \frac{(x-1)^{\frac{1}{2}}}{2^{\frac{1}{2}}}$$

② $f(x) = 2(x-1)^{\frac{2}{3}} + 4$

$$y = 2(x-1)^{\frac{2}{3}} + 4$$

$$x = 2(y-1)^{\frac{2}{3}} + 4$$

$$x - 4 = 2(y-1)^{\frac{2}{3}}$$

$$\frac{x-4}{2} = (y-1)^{\frac{2}{3}}$$

$$\left(\frac{x-4}{2}\right)^{\frac{3}{2}} = (y-1)$$

$$y = \left(\frac{x-4}{2}\right)^{\frac{3}{2}} + 1$$

③ $f(x) = 2(x-1)^{\frac{3}{2}} + 4$

$$y = 2(x-1)^{\frac{3}{2}} + 4$$

$$x = 2(y-1)^{\frac{3}{2}} + 4$$

$$x - 4 = 2(y-1)^{\frac{3}{2}}$$

$$\frac{x-4}{2} = (y-1)^{\frac{3}{2}}$$

$$\left(\frac{x-4}{2}\right)^{\frac{2}{3}} = y-1$$

$$y = \left(\frac{x-4}{2}\right)^{\frac{2}{3}} + 1$$

Jan 28-8:13 PM

Horizontal Line Test

The inverse of a function 'f' is also a function IFF no horizontal line intersects the graph 'f' more than once.

Is the inverse of this equation a function?

ex 1: Inverse is a function (hits once)

ex 2: Inverse is not a function (hits twice)

Draw a horizontal line to see intersects

Feb 8-2:25 PM

Names

$f(x)$
original function

$f^{-1}(x)$
inverse of that function

Jan 15-12:17 PM

How to verify if two functions are inverses...Compositions :)

EXAMPLE 2 Verify that functions are inverses

Verify that $f(x) = 3x - 5$ and $f^{-1}(x) = \frac{1}{3}x + \frac{5}{3}$ are inverse functions.

Solution

STEP 1 Show that $f(f^{-1}(x)) = x$.

$$f(f^{-1}(x)) = f\left(\frac{1}{3}x + \frac{5}{3}\right)$$

$$= 3\left(\frac{1}{3}x + \frac{5}{3}\right) - 5$$

$$= x + 5 - 5$$

$$= x \checkmark$$

STEP 2 Show that $f^{-1}(f(x)) = x$.

$$f^{-1}(f(x)) = f^{-1}(3x - 5)$$

$$= \frac{1}{3}(3x - 5) + \frac{5}{3}$$

$$= x - \frac{5}{3} + \frac{5}{3}$$

$$= x \checkmark$$

Jan 28-8:11 PM

#16 Verify Inverses

$f(x) = 2x + 3$ $g(x) = \frac{x-3}{2}$

1st **BOTH** **2nd**

$f(g(x)) =$ $g(f(x)) =$

$f(x) = 2x + 3$ $g(x) = \frac{x-3}{2}$ $f(x) = 2x + 3$ $g(x) = \frac{x-3}{2}$

$2\left(\frac{x-3}{2}\right) + 3$ $\frac{2x+3-3}{2}$

$x-3+3$ $\frac{2x}{2}$

x x

after simplifying if you are left w/ x **YAY!** its an inverse!

Jan 15-12:19 PM

Word Problems: The book is sketchy on what it calls an inverse...

DONT SWITCH VARIABLES- they have meaning they have value they have context... Just solve for the other variable

Gosh if its all in bold...it must be important!

Find Inverse Solve for r

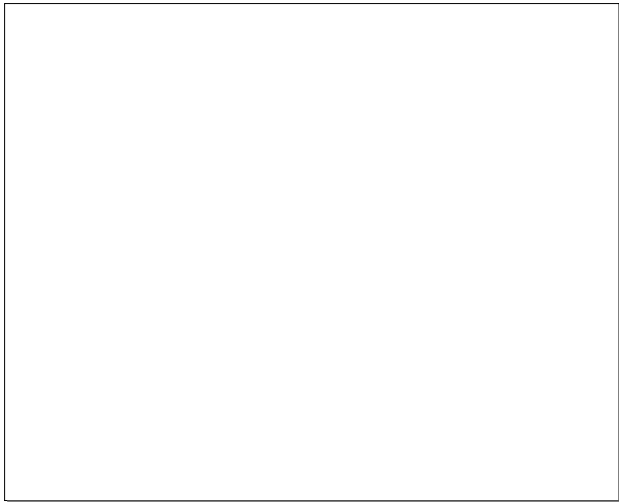
$A = \pi r^2$ **don't switch**

$A = \pi r^2$

$\sqrt{\frac{A}{\pi}} = r$

$r = \sqrt{\frac{A}{\pi}}$

Jan 17-12:54 PM



Jan 16-7:57 AM